

1. This problem is based on the Computer Graphics worksheet.
  - (a) Download the free Image Processing Toolbox through the MathWorks website, if it's not already part of your standard MATLAB installation.
  - (b) Read the documentation on `imwarp`. Show me a basic example of how it works.
  - (c) [http://starwars.wikia.com/wiki/Opening\\_crawl](http://starwars.wikia.com/wiki/Opening_crawl) Take a picture of some text, embed it in 3-dimensional space, then project until it looks right. Your pictures should be 2-dimensional – you're actually doing a projection.

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2. This problem is based on the Computer Graphics worksheet.
  - (a) The projection acts a lot like a lightbox – the point from which you're projecting is the light source, and what you see is the shadow. Take a cube, or some other shape, and draw lines extending from the projection point to the plane onto which you're projecting. You'll probably want to write a function to automate the process.
  - (b) Repeat with some other funny shape. You should get some really nice 3D pictures here; the goal is to find pictures that visually explain what projection does.

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3. This problem is based on the Curve Fitting worksheet.
  - (a) Read this: [https://www.researchgate.net/publication/247907373\\_Stupid\\_Data\\_Miner\\_Tricks\\_Overfitting\\_the\\_SP\\_500](https://www.researchgate.net/publication/247907373_Stupid_Data_Miner_Tricks_Overfitting_the_SP_500). It's moderately entertaining. The first part is interesting if you have any Stat, but the polynomial fit is the interesting bit.
  - (b) Regression often works differently at different time scales, especially for economic data. Find and import the data for the S&P 500 – probably the easiest way to do this is to download the historical data from <https://finance.yahoo.com/quote/%5EGSPC/history?p=%5EGSPC>.
  - (c) Fit a curve to the data at different scales (for example: the past week, the year 2015, stuff like that). I'd like to see a period at which the growth is well-approximated linearly, one at which it's well-approximated exponentially, and one at which it's well-approximated quadratically. These might not all exist, but I'd like to see what happens.

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4. This problem is based on the Cryptography worksheet.
- (a) There's nothing particularly special about 2 except that it's prime and that a bit is either off (0) or on (1). Most modern cryptographic algorithms use a much larger prime  $p$ , and quantum computers use qubits that can represent large primes exactly as classical computers use bits to represent arithmetic mod 2.
  - (b) Modify the functions `lfsr`, `lfsrlength`, and `lfsrsolve` to work mod  $p$ . (This means that they should now take another argument.)
  - (c) Using `imshow` like in the worksheet, show me an LFSR mod 3. You'll want to multiply by 127 rather than 255 when you `imshow` so you can see the three possible values of a trit (yes, that's the name for a "bit" which can be 0, 1, or 2). Find a length-5 base-3 LFSR of maximum period 242.
  - (d) 127 is also prime, conveniently. Find a length-2 base-127 LFSR of maximum period 16128. (Don't try to do this one visually. A length 2 LFSR is completely determined by any pair of numbers, so generate 20,000 base-127 digits with the seed data (0,1) and then search for the next time that seed appears using `find()`.)
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5. This problem is based on the Cryptography worksheet. All of the stuff you need for this one is in the Files tab.
- (a) Read Washington's notes on breaking one-time pads. He doesn't call it this, but the technique he uses is called "crib dragging."
  - (b) Show me what the `.m` files `string2bits` and `bits2string` do.
  - (c) Break the three messages.
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6. This problem is based on the Coding Theory worksheet.
- (a) Implement the Hamming (15,11) code: write down its generator and check matrix, and show me it working like you did on the fourth worksheet.
  - (b) Implement the 5-repeat code. This code is determined by  $0 \mapsto (0, 0, 0, 0, 0)$  and  $1 \mapsto (1, 1, 1, 1, 1)$ .
  - (c) `syndromedecode.m` doesn't work on the 5-repeat code because 5-repeat is 2-errors-correcting. Write a function called `repeatdecode` that can correct the errors.
  - (d) (If you're feeling extremely ambitious.) Washington's Cryptography book also describes the Hadamard code, which is a [32,6] code – that is, one with about the same coding gain as 5-repeat – with much more robust error-correcting properties. Implement the Hadamard matrix, the check matrix, and the decoding algorithm described on page 301.